

Few-Cycle Pulse Generation in an X-Ray Free-Electron Laser

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A method is proposed to generate trains of few-cycle x-ray pulses from a Free-Electron Laser (FEL) amplifier via a compact ‘afterburner’ extension consisting of several few-period undulator sections separated by electron chicane delays. Simulations show that in the hard x-ray (wavelength ~ 0.1 nm; photon energy ~ 10 keV) and with peak powers approaching normal FEL saturation (GW) levels, root mean square pulse durations of 700 zeptoseconds may be obtained. This is approximately two orders of magnitude shorter than that possible for normal FEL amplifier operation. The spectrum is discretely multichromatic with a bandwidth envelope increased by approximately two orders of magnitude over un-seeded FEL amplifier operation. Such a source would significantly enhance research opportunity in atomic dynamics, and push capability towards nuclear dynamics.

Pulses of light, tens to hundreds of attoseconds in duration, have enabled the exploration and control of processes that occur at atomic time scales [1, 2]. A common source of such pulses results from High Harmonic Generation (HHG) in a laser driven gas [3] from which isolated pulses may be generated or, more commonly, a periodic train of pulses which can act as an ultra-fast strobe. This fast stroboscopic property has been successfully applied to a range of experiments to image and control electron wave packet behaviour in atoms [4, 5]. Reducing pulse durations towards 1 attosecond, and beyond into the zeptosecond regime with high (GW) peak-powers may extend opportunities to directly resolve electronic behaviour within inner shells of atoms; the imaging and possible control of electronic-nuclear interactions such as Nuclear Excitation by Electron Transition/Capture (NEET/NEEC) [6]; and move towards the resolution of nuclear dynamics [7]. However, this will require a sufficient flux of photons with energies in the hard x-ray ($\gtrsim 10$ keV) which are not available from HHG sources.

The recently realised x-ray Free Electron Laser (FEL), which can generate the higher photon energies at multi-GW powers, would offer this enhanced temporal resolution if few-cycle, hard x-ray radiation pulses could be generated. The FEL is currently a unique source for scientific experiments, with facilities such as FLASH [8], LCLS [9], SACLA [10] and FERMI@elettra [11] in operation, and others in development [12], including proposals for a very hard x-ray source of coherent 50 keV photons [13]. The normal x-ray FEL operating mode is via a high-gain amplifier generating Self-Amplified Spontaneous Emission (SASE) [14] which has noisy temporal and spectral properties [15], although new methods are being introduced to improve on this [12]. The characteristic minimum pulse duration for such high-gain amplifier FELs is determined by the FEL bandwidth [15, 16], which for present x-ray FELs corresponds to durations $\gtrsim 100$ as. In this Letter a new operating method is proposed which, via a relatively simple upgrade, would allow existing x-ray FELs to generate trains of high-power (GW), few-cycle

pulses into the zeptosecond regime - at least two orders of magnitude shorter than currently achievable. The corresponding spectrum is discretely multichromatic within a broad bandwidth envelope. Potential applications of such sources are the stroboscopic interrogation of matter [4] with intensities enhanced by orders of magnitude compared with current sources, while the multiple narrow frequency modes may be exploited in applications such as resonant inelastic x-ray scattering [17]. High energy photon pulses of zeptosecond duration begins to make feasible access to the temporal behaviour of the nucleus, in what has been coined nuclear quantum optics [18].

In a high-gain FEL amplifier, a relativistic electron beam propagates through a long undulator, allowing a resonant, co-operative interaction with a co-propagating radiation field of resonant wavelength $\lambda_r = \lambda_u(1 + \bar{a}_u^2)/2\gamma_0^2$ [12], where λ_u is the undulator period, \bar{a}_u is the rms undulator parameter and γ_0 is the mean electron energy in units of the electron rest mass energy. The co-operative instability results in an exponential amplification of both the resonant radiation intensity and the electron micro-bunching, $b = \langle e^{-i\theta_j} \rangle$ [14], where θ_j is the ponderomotive phase [12] of the j^{th} electron. In the one-dimensional limit, the length-scale of the exponential gain is determined by the gain length $l_g = \lambda_u/4\pi\rho$, where ρ is the FEL coupling parameter [14]. A resonant radiation wavefront propagates ahead of the electrons at a rate of λ_r per λ_u . This relative propagation, or ‘slip-page’ in one gain length l_g is called the ‘co-operation length’, $l_c = \lambda_r/4\pi\rho$ [19], which determines the phase coherence length and bandwidth of the interaction.

Several methods have been proposed to generate short radiation pulses by ‘slicing’ short regions of high beam quality from within a longer electron pulse [20–23], with the shortest pulses generated at LCLS to date of $\gtrsim 1$ fs duration [24]. However, the FEL bandwidth restricts the minimum pulse length from such schemes to $\gtrsim l_c$ [15, 16], with typical value $l_c \sim 200\lambda_r$ corresponding to ~ 100 as for x-ray FELs. By inserting electron delays between modules within the long undulator, the phase coherence

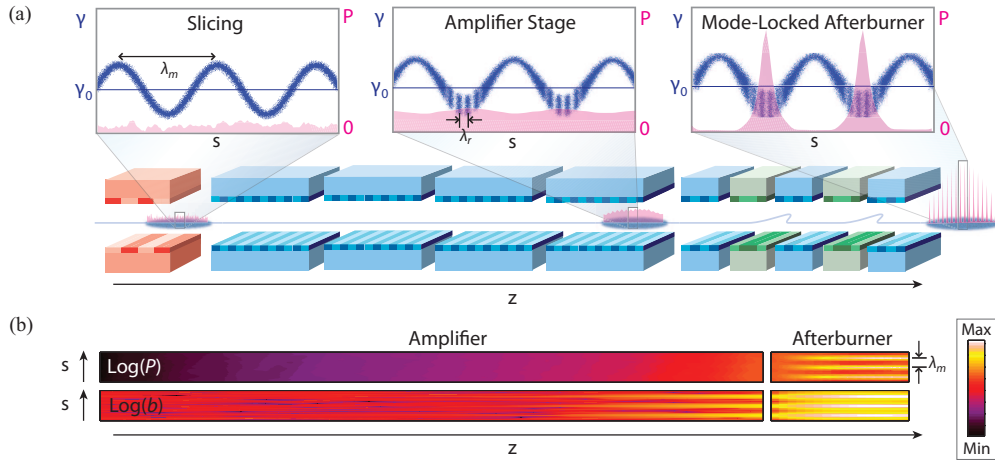


FIG. 1: (a) Schematic layout of the proposed technique and (b) Example simulation results. An electron beam is sliced (e.g. using an external laser and a short undulator to apply an energy modulation, as shown), such that a comb structure develops in the FEL-induced electron micro-bunching (b) in a long undulator (amplifier stage). Further amplification of the radiation intensity (P) with periodic electron delays (mode-locked afterburner stage) generates a train of few-cycle radiation pulses.

length of the interaction can be discretised, increasing the bandwidth. The mode-locked FEL amplifier (ML-FEL) proposal [25] uses this to generate a train of pulses with lengths $\ll l_c$ and peak powers approaching FEL saturation. The number of optical cycles per pulse is approximately the number of undulator periods per module, so could potentially deliver few-cycle pulses. However, this would require significantly modifying existing FELs, which typically have several hundred periods per module.

In this Letter, a method, shown schematically in Fig. 1, is proposed to generate trains of few-cycle radiation pulses similar to that of the ML-FEL but by using a short ‘afterburner’ extension that could relatively easily be added to existing facilities. The technique involves preparing an electron beam with periodic regions of high beam quality, each region of length $\ll l_c$, prior to injection into a normal FEL amplifier. Only these high quality regions undergo a strong FEL interaction within the amplifier to generate a periodic comb structure in the FEL-induced micro-bunching. Once the micro-bunching comb is sufficiently well developed, but before any saturation of the FEL process, the electron beam is injected into a ‘mode-locked afterburner’, which maps the comb structure of the electron micro-bunching into a similar comb of the radiation intensity. The afterburner comprises a series of few-period undulator modules separated by electron delay chicanes similar to that used in the ML-FEL [25]. These undulator-chicane modules maintain an overlap between the comb of bunching electrons and the developing radiation comb, each pulse of length $\ll l_c$, allowing it to grow exponentially in power to saturation. The pulses are delivered in trains, since amplification occurs over a number of afterburner modules, and would be naturally synchronised to the modulating laser (Fig. 1).

Several methods could be used to generate the periodically bunched electron beam prior to the afterburner, including energy modulation [20, 26], emittance spoil-

ing [22] and current enhancement [27, 28]. Here, electron beam energy modulation is used as illustrated in Fig. 1. For a sufficiently large sinusoidal energy modulation of the form $\gamma(t) = \gamma_0 + \gamma_m \cos(\omega_m t)$, where ω_m is the modulation frequency, those regions of the beam about the mean energy γ_0 will be ‘spoiled’ due to the larger energy gradients, whereas about the extrema, $\gamma \approx \gamma_0 \pm \gamma_m$, a higher beam quality exists due to smaller energy gradients. Only these latter regions may be expected to experience a strong FEL interaction within the amplifier to generate the comb structure in the electron bunching parameter. In fact, strong micro-bunching develops only at the minima of the energy modulation. It is noted from FEL linear theory [14] that there is an asymmetry about the resonant frequency for the rate of exponential gain with a critical radiation frequency below which no exponential instability exists. It may be intuitively expected that electrons about the minima will experience radiation fields generated by higher energy electrons, and so greater than their resonant frequency. Due to this gain asymmetry favouring higher frequencies these lower energy regions of the modulated beam may be expected to dominate any FEL interaction in the amplifier. This is what is observed in simulations here and in other work [26] and has also been confirmed in a more complete linear theory for an energy modulated beam [29].

Simulations of the method were carried out using the simulation code Genesis 1.3 [30] using the parameters of Table I in both the soft and hard x-ray. For the soft x-ray case, with resonant FEL wavelength of $\lambda_r = 1.24$ nm, the modulation period $\lambda_m = 38.44$ nm ($= 31\lambda_r$) and $\lambda_m \ll l_c$. This modulation could be achieved using a modulating undulator seeded by current HHG sources [2, 31]. The undulator and electron beam parameters are those of the UK New Light Source design [31]. The electron pulse length was $\gg l_c$ with no other longitudinal variation of beam parameters. The performance of the amplifier stage

TABLE I: Parameters for soft and hard x-ray simulations.

Parameter	Soft x-ray	Hard x-ray
<i>Amplifier stage</i>		
Electron beam energy [GeV]	2.25	8.5
Peak current [kA]	1.1	2.6
ρ -parameter	1.6×10^{-3}	6×10^{-4}
Normalised emittance [mm-mrad]	0.3	0.3
RMS energy spread, σ_γ/γ_0	0.007 %	0.006 %
Undulator period, λ_u [cm]	3.2	1.8
Undulator periods per module	78	277
Resonant wavelength, λ_r [nm]	1.24	0.1
Modulation period, λ_m [nm]	38.44	3
Modulation amplitude, γ_m/γ_0	0.1 %	0.06 %
Extraction point [m]	34.1	36.0
<i>Mode-locked afterburner</i>		
Undulator periods per module	8	8
Chicane delays [nm]	28.52	2.2
No. of undulator-chicane modules	~ 15	~ 40

was optimised by varying the relative amplitude, γ_m/γ_0 . The growth of the radiation power and electron bunching are plotted for a range of electron energy modulation in Fig. 2. Increasing the energy modulation amplitude decreases the region about the extrema able to lase and the mean amplification rate decreases. However, a pronounced comb in the electron bunching of period $\approx \lambda_m$ is seen to develop. Since the radiation propagates through the beam, only a relatively small undulation of the radiation power on the scale of λ_m is present. The optimum modulation amplitude was determined to be $\gamma_m/\gamma_0 \approx \rho$, with $\gamma_m/\gamma_0 = 0.1\%$ used for injection into the afterburner. The extraction point from the amplifier stage was chosen to be 34.1 m, as shown in Fig. 2. Hence, no increase in the amplifier length from that for normal saturated SASE operation is required. Both the electron beam and radiation from the amplifier stage propagate into the afterburner (Fig. 1). Each afterburner module has 8 undulator periods followed by a chicane that delays the electron beam by 23 resonant wavelengths, so that the total electron delay per module $s = (8 + 23) \times \lambda_r = \lambda_m$. Energy dispersion effects in the chicanes were included, although new chicane designs that reduce dispersive effects may be possible [32]. Figure 3 plots the radiation power and spectrum at different positions in the afterburner. A pulse train structure develops rapidly as the radiation and bunching combs are regularly re-phased by the chicanes to maintain overlap in the amplifying undulator sections. The growth within the undulator modules of the afterburner is exponential of rate comparable to that in the amplifier stage with no beam energy modulation. The growth in the afterburner is also enhanced by the additional bunching caused by the dispersive chicanes [25]. After 15 afterburner modules the output consists of a train of ~ 9 as rms radiation pulses separated by

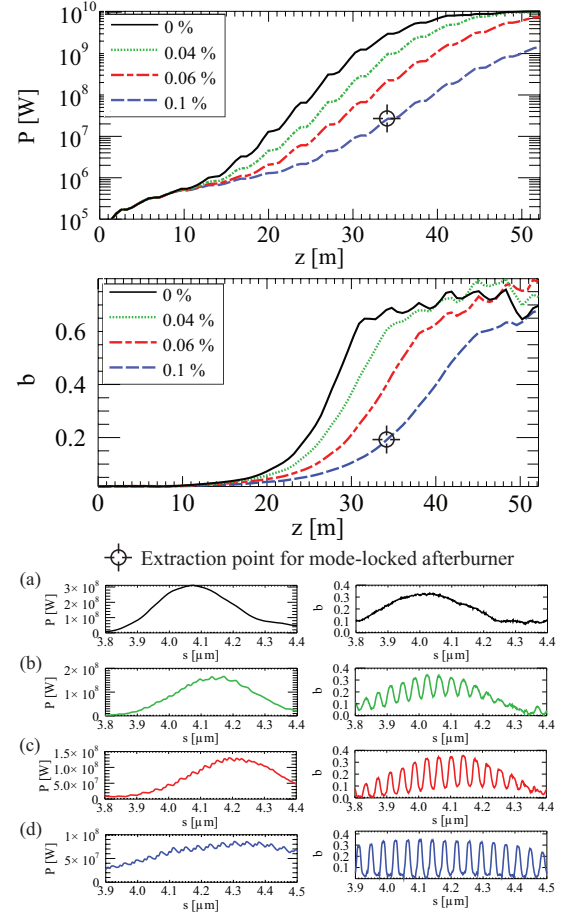


FIG. 2: Optimisation of the amplifier stage for the soft x-ray case. Maximum radiation power (top) and electron microbunching (middle) with distance through the amplifier, for different γ_m/γ_0 . Bottom panel: Longitudinal profiles of radiation (left) and bunching (right) for different γ_m/γ_0 : (a) 0 %, (b) 0.04 %, (c) 0.06 %, (d) 0.1 %. Each case is at an equivalent level of microbunching. A section of length $\sim l_c$ from a longer bunch is shown; l_c increases with increasing γ_m/γ_0 .

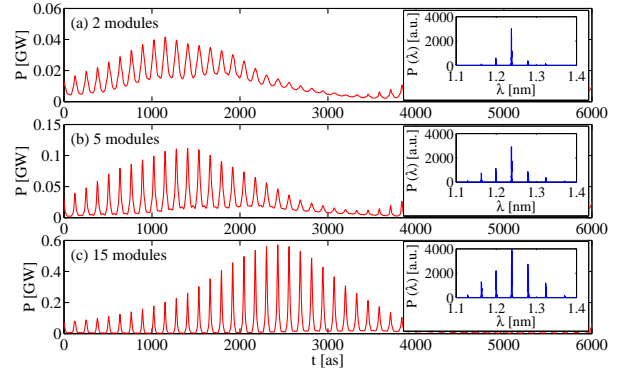


FIG. 3: Soft x-ray mode-locked afterburner simulation results: Radiation power profile and spectrum after (a) 2, (b) 5 and (c) 15 undulator-chicane modules. The duration of an individual pulse after 15 modules is ~ 9 as rms.

~ 124 as and of ~ 0.6 GW peak power. The corresponding spectrum is multichromatic with bandwidth envelope increased by ~ 50 over that of SASE. The pulse train en-

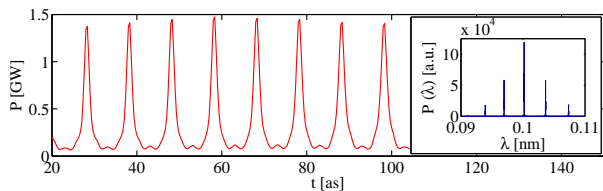


FIG. 4: Hard x-ray mode-locked afterburner simulation results: Radiation power profile and spectrum after 40 modules. The duration of an individual pulse is ~ 700 zs rms.

velope has fluctuations typical of SASE, with phase correlation between individual radiation pulses over a cooperation length. Each afterburner module consists of an undulator module of length 0.26 m and a chicane of length 0.2 m, giving a total length of 6.9 m (excluding diagnostics etc.) for the 15-module afterburner.

A hard x-ray case of resonant FEL wavelength of $\lambda_r = 0.1$ nm was also simulated, with the aim of demonstrating shorter pulse generation. A modulation period of $\lambda_m = 3$ nm was used ($\lambda_m = 30 \times \lambda_r$) which may be feasible using HHG sources that are now being developed [33]. Both the undulator and electron beam parameters used are similar to those of the compact SACLA x-ray FEL facility [10], and are detailed in Table I. A reduced peak current is used, typical for a lower electron bunch charge. This allows a slightly reduced, but still realistic, emittance to be assumed to attain a more compact afterburner stage. As for the soft x-ray case above, the amplifier stage was optimised and a beam energy modulation of $\gamma_m/\gamma_0 = 0.06$ % chosen. The amplifier section consists of six 277-period undulator modules (36 m). Each afterburner module consists of an undulator module of 8 periods and a chicane with delay of $22 \times \lambda_r$. The total electron delay per afterburner module is then equal to λ_m . The total afterburner consists of 40 modules each consisting of an undulator of length 0.144 m and a chicane of length 0.2 m to give 13.8 m in total. Figure 4 plots the radiation power and spectrum after 40 undulator-chicane modules. A pulse train structure of approximately 700 zs rms duration radiation pulses separated by 10 as and of 1.5 GW peak power is generated. The radiation mode separation is determined by the modulation period of 3 nm corresponding to photon energy difference of ≈ 412 eV. The final spectrum is multichromatic with bandwidth envelope of the modes increased by a factor ~ 100 over SASE.

Both examples in this Letter were optimised towards minimising pulse durations using parameters close to those available from current x-ray FEL sources. Using short (8-period) undulator modules in the afterburner, ~ 5 optical cycles FWHM were attained. However, the time structure could be modified by changing the number of undulator periods, electron delay lengths, and λ_m , suggesting a development route from present attosecond pulse train experiments [4, 5] to the ultimate capability of the scheme. Amplification in the afterburner was set to occur just before saturation, allowing a short after-

burner to attain high contrast ratio of the pulse train over the amplifier radiation. Further development to maximise the peak power and flexibility of the pulse structure could include investigation of saturation effects in the afterburner (e.g. chicane dispersion, radiation diffraction) and their mitigation through e.g. undulator tapering [34], optimised phase-shifting [35], use of low-dispersion [32] or more compact chicanes. Methods to improve the temporal coherence and stability developed for SASE, may also be applicable. A potential proof-of-principle experiment would be to use a single-module afterburner [36]. This is similar to other proposals [37, 38] to attain pulse lengths $\ll l_c$, but at relatively low power, since they operate via coherent spontaneous emission in a single short undulator, rather than exponential amplification.

If the above results are scaled to higher photon energies, e.g. to the 50 keV of the proposed x-ray FEL of [13], then pulse durations of 140 zs rms may become feasible. Operation at harmonics of λ_r may be another route to shorter pulse durations. Furthermore, if a relativistic counter-propagating target nuclear beam were used with such pulse trains, as discussed in [18], in addition to the increased doppler-shifted photon energies that the nuclei experience in their boosted frame, the pulse durations may be further reduced towards the timescales of highly ionised heavy elements and nuclear dynamics [7].

The mode-locked afterburner is potentially a relatively simple upgrade to existing x-ray FEL facilities. It offers a flexible route towards the generation of discretely multichromatic output under a broad bandwidth envelope, and so offers few-cycle x-ray pulse trains with GW peak-powers in the temporal domain. This would help facilitate the direct study of the temporal evolution of complex correlated electronic behaviour within atoms, and push capability into the regime of electronic-nuclear dynamics and towards that of the nucleus.

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